

$$\frac{1}{2}(\cos(x-P/4) - \cos(3x+P/4))=1$$

$$\cos(x-P/4) - \cos(3x+P/4)=2$$

$$\cos(x-P/4)=1$$

$$\cos(3x+P/4)=-1$$

$$x-P/4=2pk$$

$$x=2pk+p/4$$

$$3x+P/4=p+2pk$$

$$3x=3p/4+2pn$$

$$x=p/4+2pn/3$$

$$2pk+p/4=p/4+2pn/3$$

$$2k+\frac{1}{4}=\frac{1}{4}-2n/3$$

$$24k+3=3-8n$$

$$24k-8n=0$$

$$24k=8n$$

$$3k=n$$

$$x=p/4+2pk$$

Ответ: $p/4+2pk$